

MATH 302 WORKSHEET IV SPRING 2010 NAME: \_\_\_\_\_  
(PLEASE PRINT LEGIBLY)

1. Let  $X, Y \sim w((x,y))$  such that  $w((x,y)) = \begin{cases} \frac{3}{2}x^2(1-|y|) & -1 \leq x \leq 1, \quad -1 \leq y \leq 1 \\ 0 & \text{else} \end{cases}$

- A. Find  $\mu_X$                       B. Find  $\mu_Y$                       C. Find  $\sigma_X^2$   
D. Find  $\sigma_{XX}$                       E. Find  $\sigma_{XY}$

2. Let  $X, Y \sim p((x,y))$  be defined such that

$$p((x,y)) = \begin{cases} \frac{n!}{x!y!(n-x-y)!} \cdot p_1^x \cdot p_2^y \cdot (1-p_1-p_2)^{n-x-y} & x \in \mathbb{N}^* \quad y \in \mathbb{N}^* \quad x+y \leq n \\ 0 & \text{else} \end{cases}$$

Let  $p_1 = \frac{1}{5}$ ,  $p_2 = \frac{2}{5}$ , and  $n = 5$

- A. Find  $\mu_X$                       B. Find  $\mu_Y$                       C. Find  $\sigma_X^2$   
D. Find  $\sigma_{XX}$                       E. Find  $\sigma_{XY}$

3. Let  $X, Y \sim m((x,y))$  be defined such that

$$m((x,y)) = \begin{cases} \frac{x+y}{32} & x \in \mathbb{N}_2, \quad y \in \mathbb{N}_4 \\ 0 & \text{else} \end{cases}$$

- A. Find  $\mu_X$                       B. Find  $\mu_Y$                       C. Find  $\sigma_X^2$   
D. Find  $\sigma_{XX}$                       E. Find  $\sigma_{XY}$

4. Let  $X, Y \sim g((x,y))$  be defined such that

$$g((x,y)) = \begin{cases} \frac{1}{16} e^{-\left(\frac{x+y}{2+8}\right)} & x \in [0, \infty) \quad y \in [0, \infty) \\ 0 & \text{else} \end{cases}$$

- A. Find  $\mu_X$                       B. Find  $\mu_Y$                       C. Find  $\sigma_X^2$   
D. Find  $\sigma_{XX}$                       E. Find  $\sigma_{XY}$

5. Let  $X, Y$  be jointly distributed such that the joint probability mass function,  $k_{xy}((x, y))$  is defined as:

$$k_{xy}((x, y)) = \begin{cases} \frac{x+y}{21} & x \in \mathbb{N}_3 \quad y \in \mathbb{N}_2 \\ 0 & \text{else} \end{cases}$$

- A. Find  $\mu_X$                       B. Find  $\mu_Y$                       C. Find  $\sigma_X^2$   
D. Find  $\sigma_{XX}$                       E. Find  $\sigma_{XY}$