

## Handout 4 $\frac{31}{32}$

The Ponis Claims To Think About Which May Be of Use  
for Basic Analytic, Number Theoretic, or Algebraic Proofs

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Let our universe be  $\mathbb{R}$ .

Claim P.1:  $\forall x \in \mathbb{R}, y \in \mathbb{R}, z \in \mathbb{R}$ , it is the case that  $x \neq y \implies x + z \neq y + z$ .

Claim P.2:  $\forall x \in \mathbb{R}, y \in \mathbb{R}, z \in \mathbb{R}$ , it is the case that  $(xz < yz) \implies ((x < y) \wedge (z > 0))$ .

Claim P.3:  $\forall x \in \mathbb{R}, y \in \mathbb{R}, z \in \mathbb{R}$ , it is the case that  $(xz < yz) \implies (((x < y) \wedge (z < 0)) \vee ((x > y) \wedge (z < 0)))$ .

Claim P.4<sup>1</sup>:  $x \in \mathbb{N} \wedge y \in \mathbb{N} \implies (x - y) \in \mathbb{N}$ .

Claim P.5<sup>2</sup>:  $x \in \mathbb{N} \wedge y \in \mathbb{N} \implies \neg((x - y) \in \mathbb{N})$ .

Claim P.5:  $x \in \mathbb{N} \wedge y \in \mathbb{N} \implies (x - y) \notin \mathbb{N}$ .

The challenge: Try to prove or disprove these claims.

These were claimed (devised or thought of) by Mr. Ponis who is in the 2 P.M. MWF class. They are fun.

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<sup>1</sup>We prove this false in the 2 P.M. MWF class.

<sup>2</sup>This is poorly written.