

**Worksheet I2**  
Beginning Sets  
and  
Analytic Claims  
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10. PROVE OR DISPROVE (ANALYTIC CLAIMS)

**Claim 10.1.**  $U = \mathbb{R}$ . Let  $x \in \mathbb{R} \wedge x > 0$  It is the case that  $\frac{1}{x} > 0$ .  
*Prove or disprove the claim.*

**Claim 10.2.**  $U = \mathbb{R}$ . Let  $x \in \mathbb{R} \wedge y \in \mathbb{R} \ni x < y$ . It is the case that  $\frac{1}{x} > \frac{1}{y}$ .  
*Prove or disprove the claim.*

**Claim 10.3.**  $U = \mathbb{R}$ . Let  $x \in \mathbb{R} \wedge y \in \mathbb{R} \ni x > 0$  and  $y \leq 0$ . It is the case that  $x \cdot y \leq 0$ .  
*Prove or disprove the claim.*

Prove or disprove the following:

**Claim 10.4.**  $U = \mathbb{R} \ x \cdot 0 = 0$ .

**Claim 10.5.**  $U = \mathbb{R} \ x \in \mathbb{R}. \ x^2 > 0$ .

**Claim 10.6.**  $U = \mathbb{R} \ x \in \mathbb{R}. \ x^2 \geq 0$ .

**Claim 10.7.**  $U = \mathbb{R} \ x < 0 \wedge y > 0$  implies  $x \cdot y < 0$ .

**Claim 10.8.**  $U = \mathbb{R} \ x < 0 \wedge y > 0$  implies  $x + y < 0$ .

Comment: " $\infty$ " is not a real number.