

**Worksheet IIA**  
**PRE-CALCULUS GRAPHING**  
 AND  
**CRUNCHING OF SOME VALUES OF A FUNCTION AT CERTAIN X-VALUES**  
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Questions and Exercises

1. Consider  $k : \mathbb{R} \rightarrow \mathbb{R}$  where

$$k(x) = \begin{cases} 3x + 15, & x < -2 \\ \frac{1}{x-1}, & -2 \leq x < 1 \\ 3, & x = 1 \\ \frac{4}{(x+2)^2}, & 1 < x < 3 \\ (x+1)^3, & x \geq 3 \end{cases}$$

- A. Find the domain of  $k$ .      B. Find the codomain of  $k$ .  
 C. Graph  $k$ .                      D. Find the range of  $k$ .

2. Consider  $j : \mathbb{R} \rightarrow \mathbb{R}$  where

$$j(x) = \begin{cases} \sin(x), & x < -\frac{\pi}{2} \\ e^x, & -\frac{\pi}{2} \leq x \leq 0 \\ x^4, & 0 < x \leq 2 \\ -2x^2, & 2 < x \end{cases}$$

- A. Find the domain of  $j$ .      B. Find the codomain of  $j$ .  
 C. Graph  $j$ .                      D. Find the range of  $j$ .

3. Consider  $p : \mathbb{R} \rightarrow \mathbb{R}$  where

$$p(x) = \begin{cases} 5x - 2, & x < -1 \\ \frac{1}{3}, & x = -1 \\ \cos(x), & -1 < x < 2 \\ \ln(x), & x \geq 2 \end{cases}$$

- A. Find the domain of  $p$ .      B. Find the codomain of  $p$ .  
 C. Graph  $p$ .                      D. Find the range of  $p$ .

4. Consider  $m : \mathbb{R} \rightarrow \mathbb{R}$  where

$$m(x) = \begin{cases} \arctan(x), & x < \frac{1}{\sqrt{3}} \\ 4x - 8, & x \geq \frac{1}{\sqrt{3}} \end{cases}$$

- A. Find the domain of  $m$ .      B. Find the codomain of  $m$ .  
 C. Graph  $m$ .                      D. Find the range of  $m$ .

5. Consider  $q : (0, \infty) \rightarrow \mathbb{R}$  where

$$q(x) = \begin{cases} \ln(x), & x < 1 \\ 3x - 3, & x \geq 1 \end{cases}$$

- A. Find the domain of  $q$ .      B. Find the codomain of  $q$ .  
C. Graph  $q$ .                      D. Find the range of  $q$ .

6. Let

$$f(x) = \begin{cases} \frac{x^2-1}{x-1}, & x \neq 1 \\ 3, & x = 1 \end{cases}$$

where  $f : \mathbb{R} \rightarrow \mathbb{R}$

- A. Find  $f(3)$ ,  $f(2)$ ,  $f(\frac{3}{2})$ ,  $f(\frac{5}{4})$ ,  $f(\frac{9}{8})$ ,  $f(\frac{17}{16})$ ,  $f(1.01)$ ,  $f(1.001)$ , and  $f(1.0001)$ .  
B. Find  $f(-3)$ ,  $f(\pi)$ ,  $f(\sqrt{2})$ ,  $f(\frac{1}{2})$ ,  $f(\frac{3}{4})$ ,  $f(\frac{63}{64})$ ,  $f(0.99)$ ,  $f(0.999)$ , and  $f(1)$ .