

Let $U = S = \mathbb{Z}$ (the sample space is the integers).

Let the data be described as X_1, X_2, X_3, X_4 (as in problem 1), as X_1, X_2, X_3, X_4, X_5 (as in problem 2) etc.

1. Let the data set be $D_1 = \{1, 2, 3, 4\}$

Find:

- | | | |
|---|------------------------------------|---|
| A. the mode of the sample | B. The median of the sample | C. the arithmetic mean (sample mean) of the sample. |
| D. the geometric mean of the sample. | | E. the harmonic mean of the sample. |
| F. find the deviation of X_1 | G. find the variance of the sample | H. find the standard deviation of the sample |
| I. find the mean absolute deviation (MAD) | | J. find the range |

2. Let the data set be $D_2 = \{1, 2, 2, 3, 4\}$

Find:

- | | | |
|--------------------------------|------------------------------------|--|
| F. find the deviation of X_1 | G. find the variance of the sample | H. find the standard deviation of the sample |
|--------------------------------|------------------------------------|--|

3. Let the data set be $D_3 = \{1, 2, 3, 3, 4\}$

Find:

- | | | |
|--------------------------------|------------------------------------|--|
| F. find the deviation of X_1 | G. find the variance of the sample | H. find the standard deviation of the sample |
|--------------------------------|------------------------------------|--|

4. Let the data set be $D_4 = \{1, 3, 3, 3, 4\}$

Find:

- | | | |
|---|------------------------------------|--|
| F. find the deviation of X_1 | G. find the variance of the sample | H. find the standard deviation of the sample |
| I. find an approximation for the standard deviation to accurate to 3 significant figures. | | |

5. Flip a fair coin 4 times and record the number of heads. Let H be the number of heads obtained. Then

$$H \sim j(h) \text{ where } j(h) \text{ a probability mass function (pmf) such that } j(h) = \begin{cases} \binom{4}{h} \cdot \left(\frac{1}{2}\right)^h \cdot \left(\frac{1}{2}\right)^{(4-h)} & h \in \mathbb{N}_4^* \\ 0 & \text{else} \end{cases}$$

explicitly find all the probabilities (in chart form) and graph the pmf.

6. Flip a non-fair coin 4 times and record the number of heads. Let the probability of tossing a head be $\frac{1}{5}$ Let H be the number

of heads obtained. Then $H \sim k(h)$ where $k(h)$ a probability mass function (pmf) such that

$$k(h) = \begin{cases} \binom{4}{h} \cdot \left(\frac{1}{5}\right)^h \cdot \left(\frac{4}{5}\right)^{(4-h)} & h \in \mathbb{N}_4^* \\ 0 & \text{else} \end{cases} \text{ explicitly find all the probabilities (in chart form) and graph the pmf.}$$

7. What is the difference (if any) with the arithmetic mean, standard deviation, skewness, or kurtosis between and betwixt problem 5 and 6 (DO NOT COMPUTE THE VALUES OF THE arithmetic mean, standard deviation, skewness, or kurtosis just opine from the graphs).

8. Take a coin and flip it 4 times record the number of heads. Do this 20 times and send the results to me at mcloughl@kutztown.edu (a list of 20 numbers all in \mathbb{N}_4^* in *.txt form please).